Superconductivity - Overview

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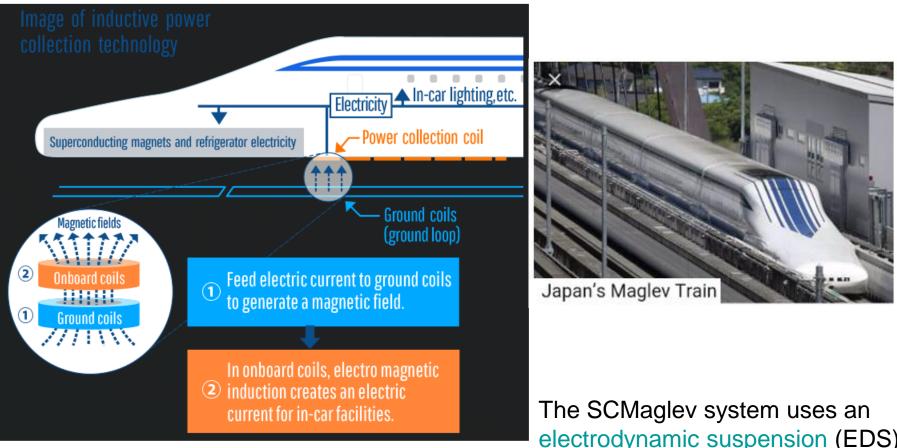


Importance of superconductivity: Qubits and modern quantum computers are made of superconductors

IBM Q



Superconducting-magnet levitation train



The <u>L0 Series</u>, a prototype vehicle based on SCMaglev technology, holds the record for fastest crewed rail vehicle with a record speed of 603 km/h (375 mph). Time Urbana-Chicago: only ~25 min The SCMaglev system uses an <u>electrodynamic suspension</u> (EDS) system. The train's <u>bogies</u> have <u>superconducting</u> magnets installed, and the guideways contain two sets of metal coils.

Superconducting magnets for MRI

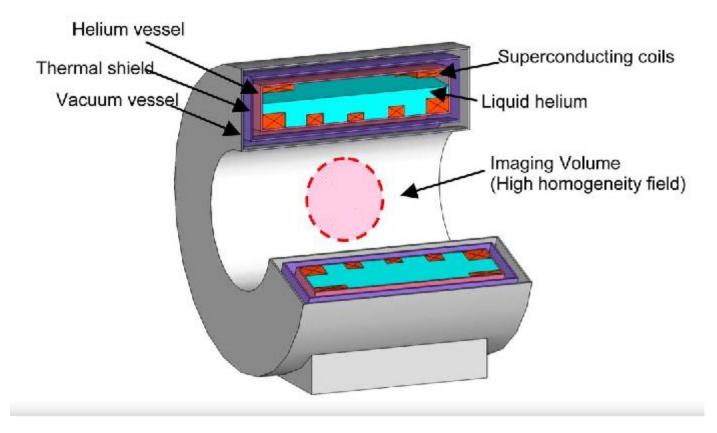


Fig. 2. Cross-sectional view of the magnet.



P

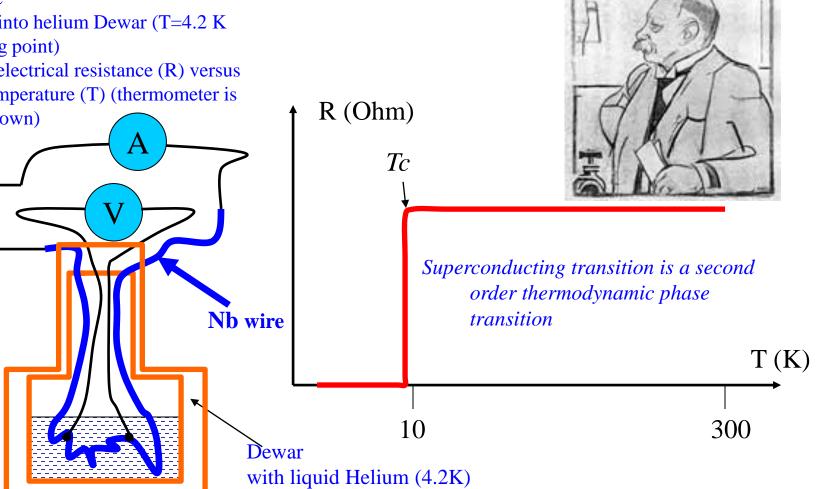
How to measure superconducting transitions

Electrical resistance of some metals drops to zero below a certain temperature which is called "critical temperature" (H. K. O. 1911)

How to observe superconductivity

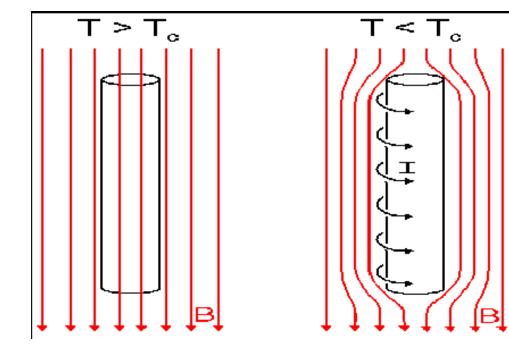
- 1. Take Nb (niobium) wire
- 2. Connect to a voltmeter and a current source
- 3. Immerse into helium Dewar (T=4.2 K boiling point)
- 4. Measure electrical resistance (R) versus the temperature (T) (thermometer is not shown)

Heike Kamerling Onnes





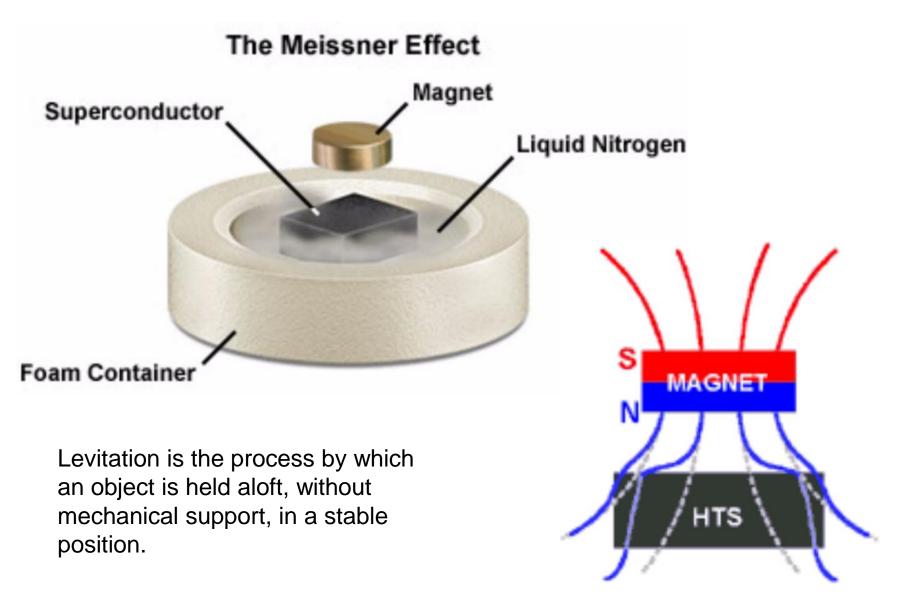
Meissner effect – the key signature of superconductivity



Theory of superconductivity: "BCS" – due to Bardeen, Cooper and Schrieffer

Formula	т _с (К)	$H_{\rm C}\left({\rm T} ight)$	Туре	BCS
Elements				
AI	1.20	0.01	I	yes
Cd	0.52	0.0028	I	yes
Diamond:B	11.4	4	II	yes
Ga	1.083	0.0058	I	yes
Hf	0.165		I	yes
a-Hg	4.15	0.04	I	yes
β-Hg	3.95	0.04	I	yes
In	3.4	0.03	I	yes
Ir	0.14	0.0016 ^[7]	I	yes
α-La	4.9		I	yes
β-La	6.3		I	yes
Мо	0.92	0.0096	I	yes
Nb	9.26	0.82	II	yes
Os	0.65	0.007	I	yes

Interesting phenomenon: Magnetic levitation



https://nationalmaglab.org/magnet-academy/read-science-stories/science-simplified/superconductivity-101/

BCS Theory - the origin of superconductivity

Bardeen Cooper and Schrieffer derived two expressions that describe the mechanism that causes superconductivity,

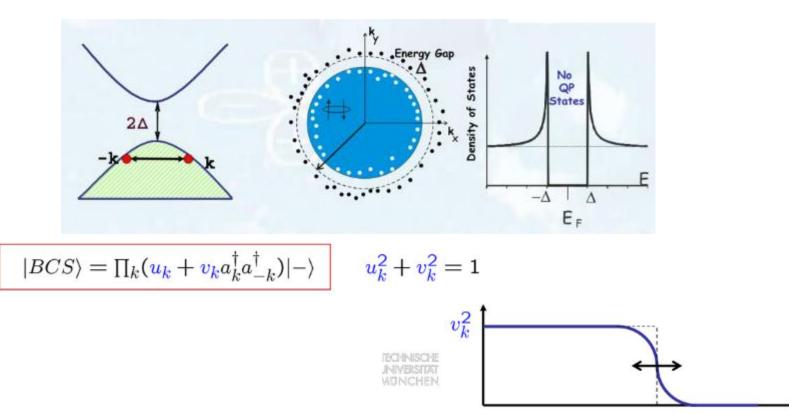
$$|\Delta| = 2\hbar\omega_D \exp\left[-\frac{1}{N(0)V}\right]$$
$$z_B T_c = 1.14\hbar\omega_D \exp\left[-\frac{1}{N(0)V}\right]$$

where Tc is the critical temperature, Δ is a constant energy gap around the Fermi surface, N(0) is the density of states and V is the strength of the coupling.









 ε_k

Author: Jure Kokalj Mentor: prof. dr. Peter Prelovšek

https://www.slideserve.com/connie/unconventional-superconductivity

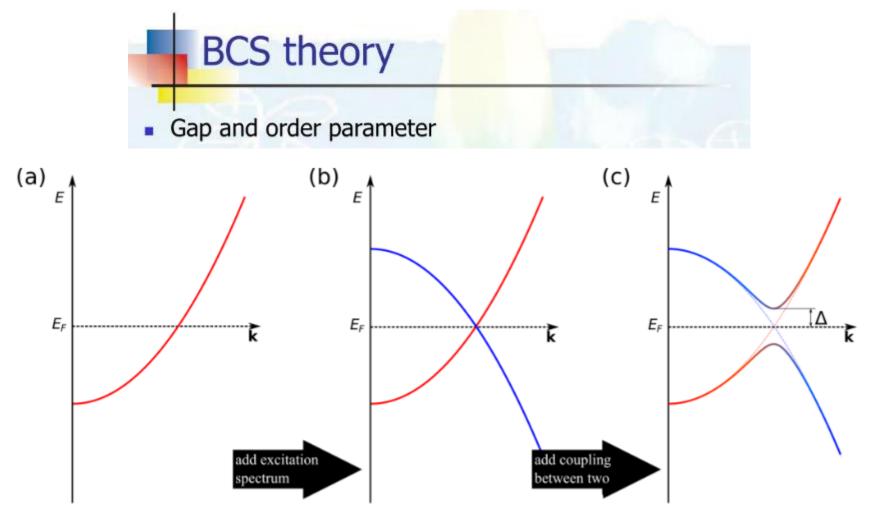
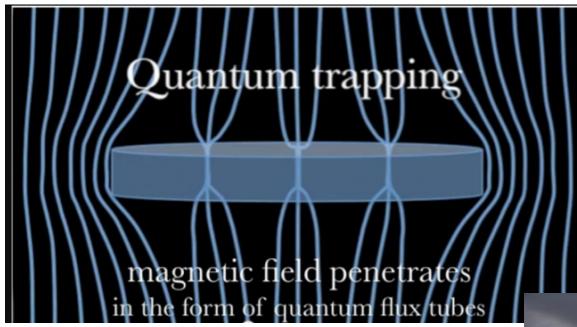


Figure 1: BCS theory: example of electron and hole bands coupling. (a) a parabolic electron-like band, (b) add the excitation hole-like band, (c) superconducting gap opens when the electron-like and hole-like bands are coupled by an interaction Δ .

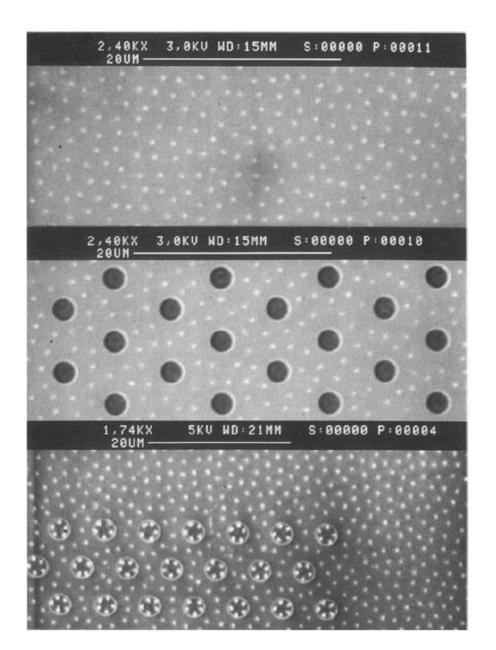
Magnetic field effect: Superconducting vortices



https://blog.tmcnet.com/blog/tomkeating/technology-and-science/quantumlevitation-back-to-the-futurehoverboard.asp In superconductivity, a **fluxon** (also called an **Abrikosov vortex** or **quantum vortex**) is a vortex of <u>supercurrent</u> in a <u>type-II superconductor</u>s



Vortices in superconducting films with "through" and "blind" holes ("antidots")

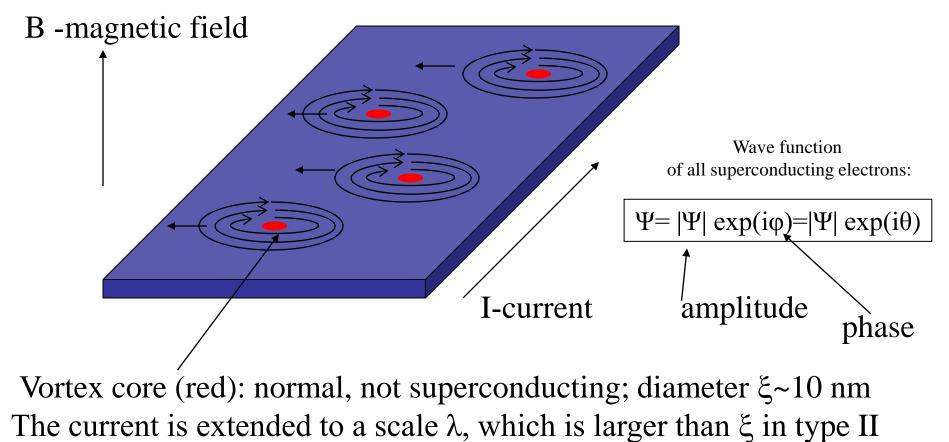


A. Bezryadin and B. Pannetier "Role of Edge Superconducting States in Trapping of Multi-Quanta Vortices by Microholes. Application of the Bitter Decoration Technique", J. Of Low Temp. Phys., V.102, p.73 (1996).

Vortices are quantized tubes carrying magnetic field into superconductor

Magnetic field creates vortices--

Vortices cause dissipation (i.e. a non-zero electrical resistance), if they move



superconductors (such as thin films of any material)

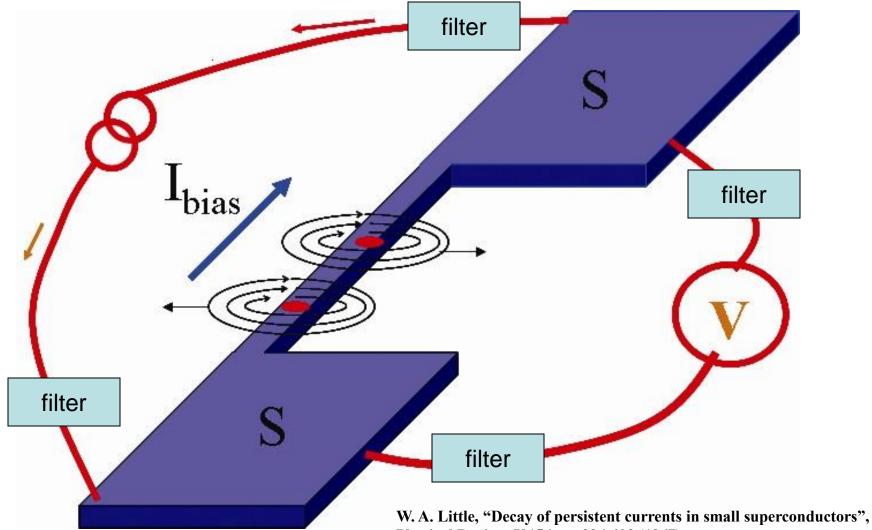
Reminder: single electron in empty space

Wave function: $\Psi = |\Psi| \exp(i\mathbf{kx}) = |\Psi| [\cos(\mathbf{kx}) + i \sin(\mathbf{kx})]$ Wave number: $\mathbf{k}=2\pi/\lambda$ $i^*i=-1$

General form: $\Psi = |\Psi| \exp(-i\varphi)$ In this example of a plane wave, the phase is: $\varphi = kx$

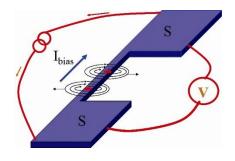
DC transport measurement schematic to detect passing vortices

Bleu: superconducting film and wire Red: Phase slip events or crossing vortices



Physical Review, V.156, pp.396-403 (1967).

How to use voltage to determine the rate of phase slips?



Key principle: every time a vortex crosses the wire the phase difference changes by 2π .

Phase evolution equation: $d\phi/dt = 2eV/\hbar$

Simplified derivation:

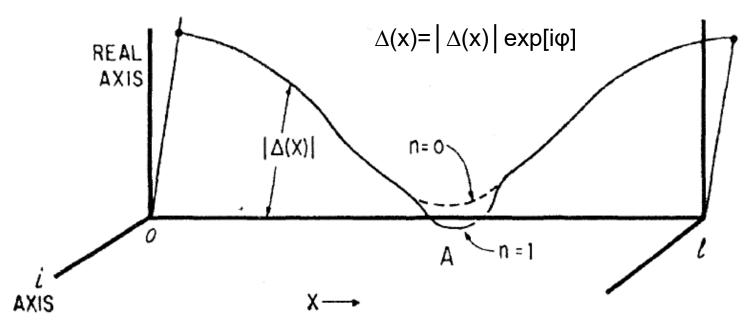
- 1. Time-dependent Schrödinger equation with fixed energy: $i\hbar(d\Psi/dt)=E \Psi$
- 2. The solution is: $\Psi = \exp(-iEt/\hbar)$ (here E is the energy)
- 3. The phase of the wavefunction is $\varphi = Et/\hbar$

4. The energy is defined by the electric potential (voltage), V as follows: E=2eV. Note that the effective charge of superconducting electrons is 2e, where "e" is the charge of one electron. Such superconducting electron pairs are called Cooper pairs.

Thus, the resulting equation is: $d\phi/dt = 2eV/\hbar$

Gor'kov, L.P. (1958) Sov. Phys. JETP, 7, 505.

Thin superconducting wire have some nonzero electrical resistance due to Little's Phase Slips

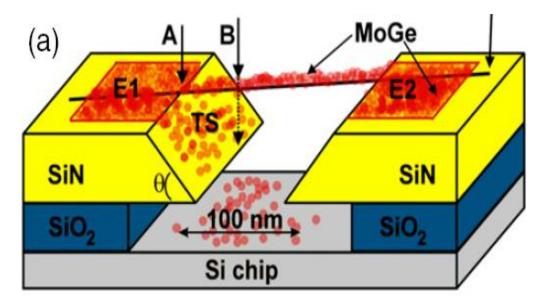


W. A. Little, "Decay of persistent currents in small superconductors", Physical Review, V.156, pp.396-403 (1967).

Two types of phase slips (PS) can occur:1. The usual, thermally activated PS (TAPS)2. Quantum phase slip (QPS)

Fabrication of nanowires

Method of Molecular Templating



Si/SiO₂/SiN substrate with undercut

~ 0.5 mm Si wafer 500 nm SiO₂ 60 nm SiN Width of the trenches ~ 50 - 500 nm

HF wet etch for ~10 seconds to form undercut

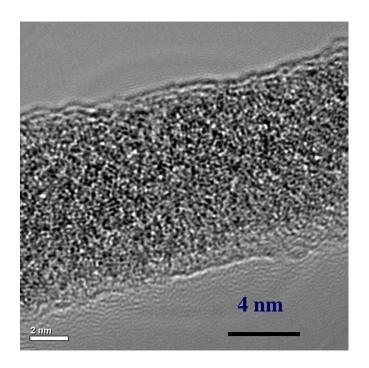
В

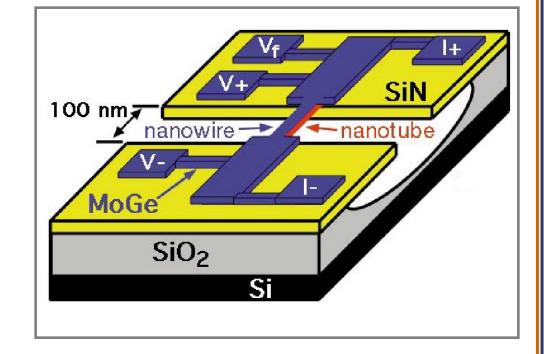
200 nm

(b)

Bezryadin, Lau, Tinkham, Nature 404, 971 (2000)

Sample Fabrication





TEM image of a wire shows amorphous wire morphology. Nominal MoGe thickness = 3 nm Schematic picture of the pattern Nanowire + Film Electrodes used in transport measurements



Dichotomy in nanowires: Evidence for superconductorinsulator transition (SIT)

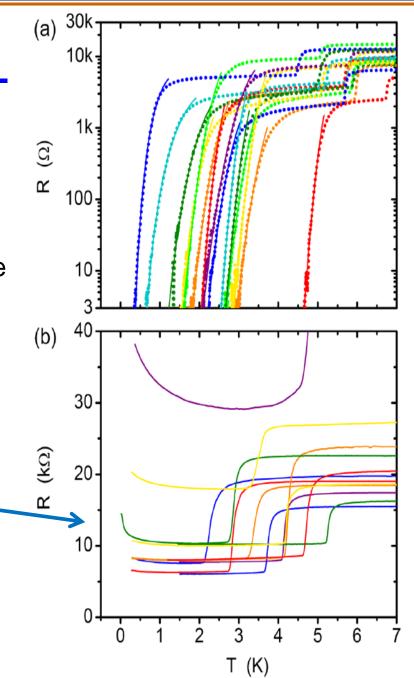
R = V/I I~3 nA

The difference between samples is the amount of the deposited Mo79Ge21.

Thin wires become insulating if their normal resistance is lager than resistance quantum h/4/e/e=6.5KOhm

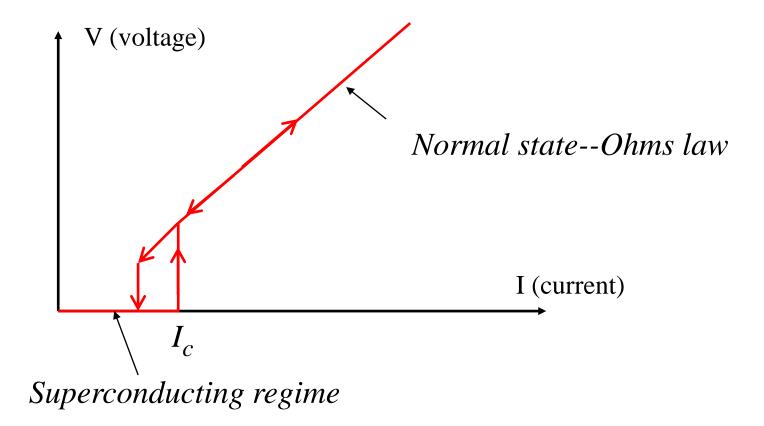
The insulating behavior is due to proliferation of quantum phase slips

Bollinger, Dinsmore, Rogachev, Bezryadin, Phys. Rev. Lett. **101**, 227003 (2008)

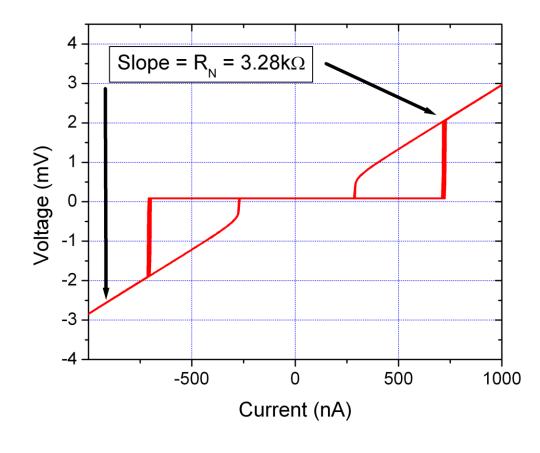


Expected voltage-current curve

Electrical resistance is zero only if current is not too strong

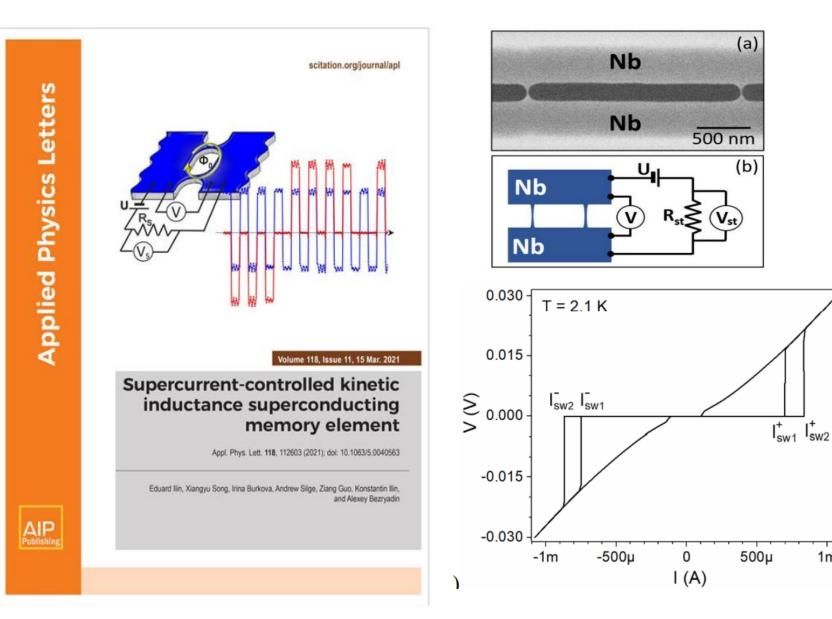


Experimental voltage-current curve. Fluctuations of the switching current are due to Little's phase slips





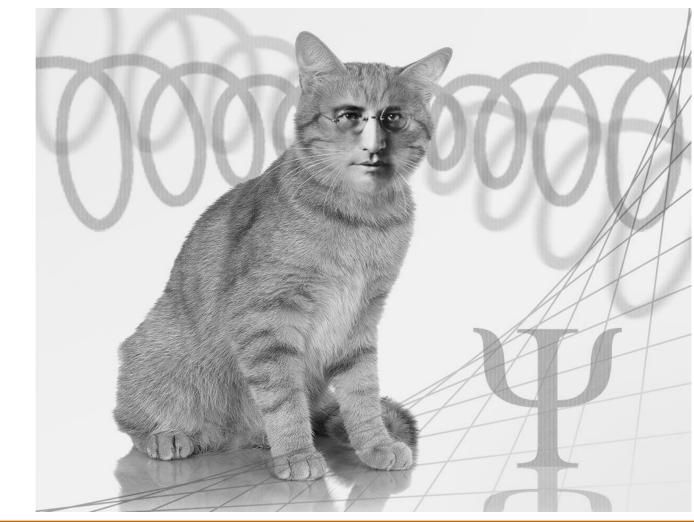
Superconducting nanowire memory



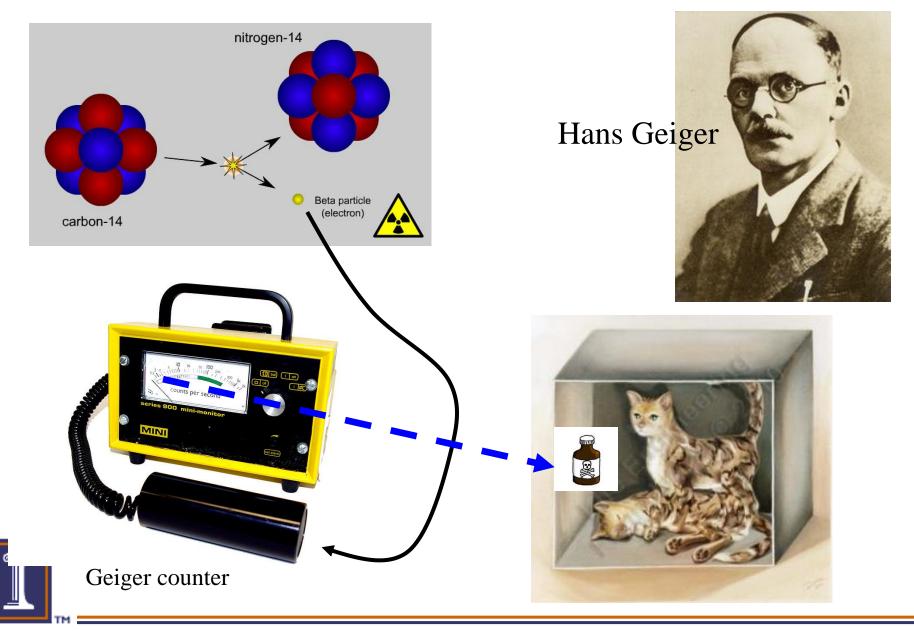
1m

Schrödinger cat – the ultimate macroscopic quantum phenomenon

E. Schrödinger, Naturwiss. 23 (1935), 807.



Schrödinger cat – thought experiment





Linearity of the Schrödinger's equation

Suppose Ψ_1 is a valid solution of the Schrödinger equation: $i\hbar \frac{\partial \psi_1}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \psi_1}{\partial x^2} + U(x)\psi_1$

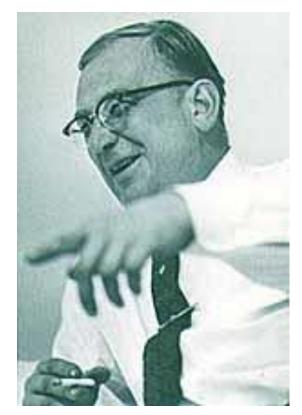
And suppose that Ψ_2 is another valid solution of the Schrödinger equation:

$$i\hbar\frac{\partial\psi_2}{\partial t} = -\frac{\hbar^2}{2m}\frac{\partial^2\psi_2}{\partial x^2} + U(x)\psi_2$$

Then $(\Psi_1 + \Psi_2)/\sqrt{2}$ is also a valid solution, because:

 $i\hbar \frac{\partial(\psi_1 + \psi_2)}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2(\psi_1 + \psi_2)}{\partial x^2} + U(x)(\psi_1 + \psi_2)$ The state $(\Psi_1 + \Psi_2)/\sqrt{2}$ is a new combined state which is called "quantum superposition" of state (1) and (2)

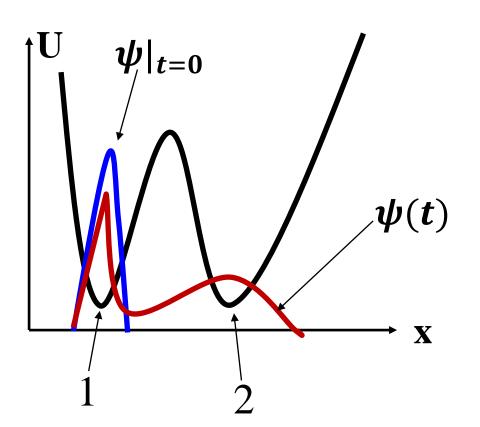




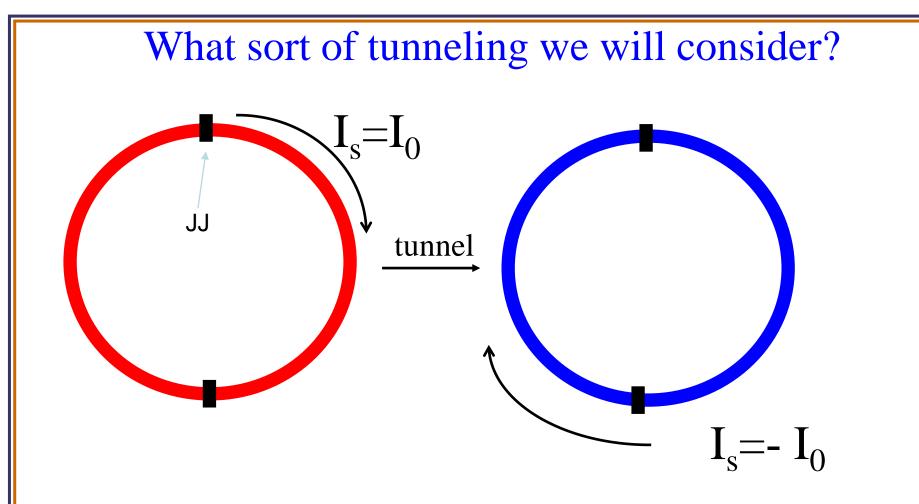
George Gamow

(He also helped to developed Big Bang theory)

Quantum tunneling



Quantum tunneling is possible since quantum superpositions of states are possible.



-Red color represents some strong current in the superconducting wire loop

-Blue color represents zero current in the loop



Types of Qubit

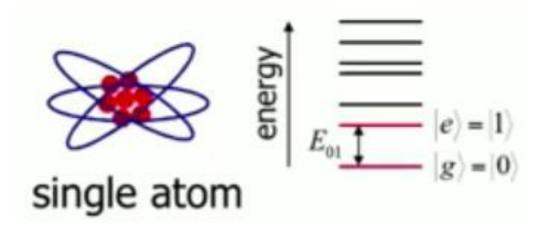
$$\int \frac{|\downarrow\rangle = |1\rangle}{|\uparrow\rangle = |0\rangle}$$

single spin-1/2

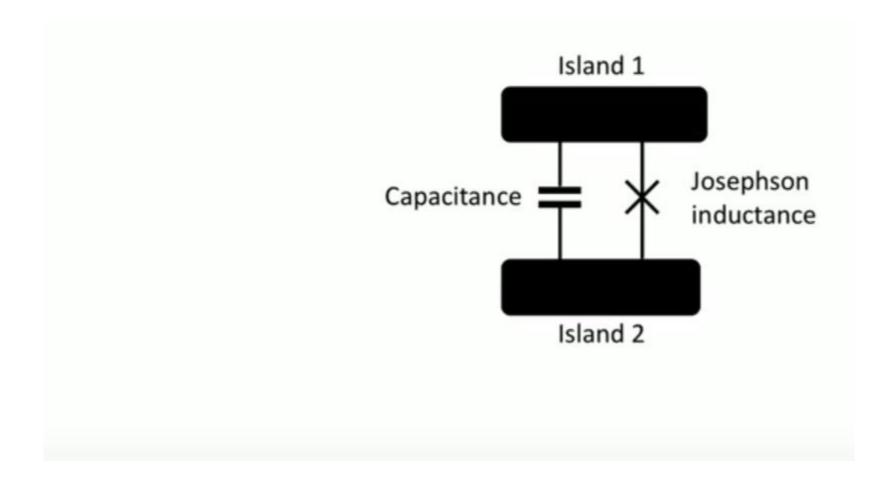
Quantum state: $|\psi\rangle = A^*|0\rangle + B^*1\rangle$

 $A^2+B^2=1$

A and B are complex numbers



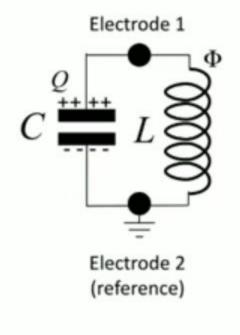
Transmon Qubit



Theory of transmons: J. Koch et al., Phys. Rev. A 76, 042319 (2007).

Quantization of electrical circuits

The quantized LC oscillator



Hamiltonian:

$$\hat{H}_{LC} = \frac{\hat{Q}^2}{2C} + \frac{\hat{\Phi}^2}{2L}$$
Capacitive term Inductive term

Canonically conjugate variables:

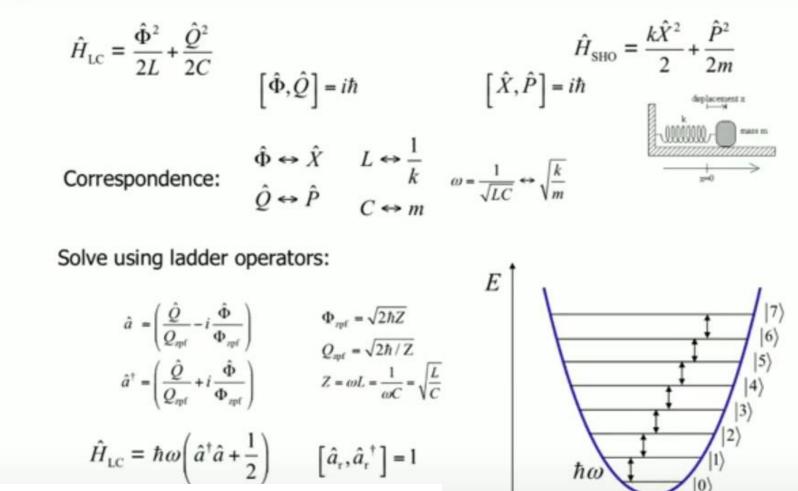
- $\hat{\Phi}$ = Flux through the inductor.
- \hat{Q} = Charge on capacitor plate.

$$\left[\hat{\Phi},\hat{Q}\right] = i\hbar$$

M. Devoret, Les Houches Session LXIII (1995)

Discrete energy spectrum of the LC-circuit

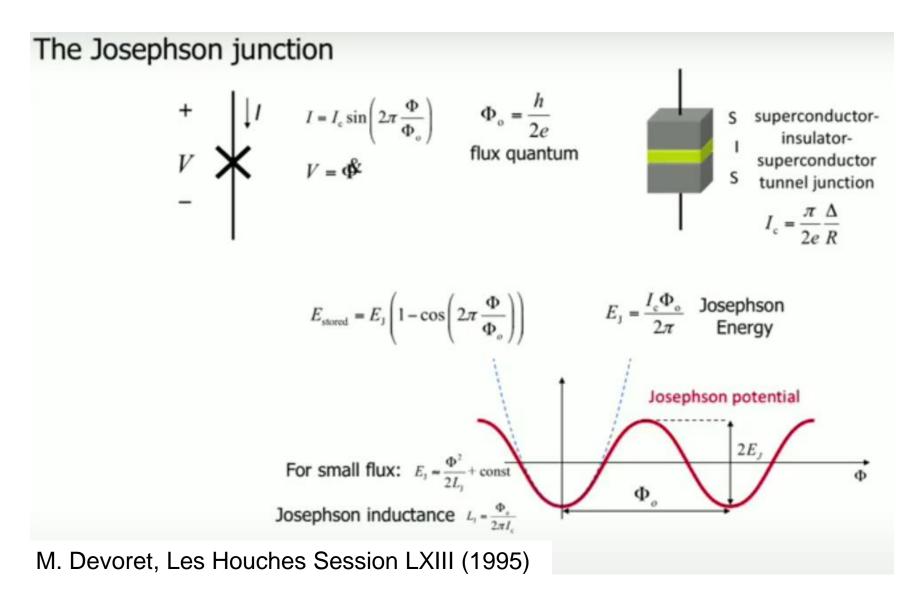
Correspondence with simple harmonic oscillator



Φ

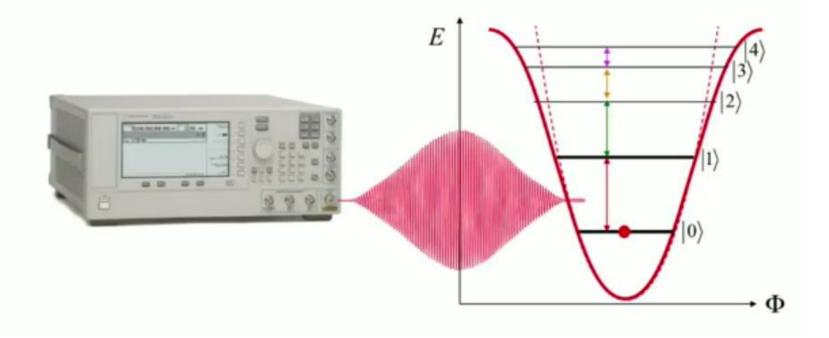
M. Devoret, Les Houches Session LXIII (1995)

Non-harmonicity is the key factor



Non-harmonicity is the key factor

Transmon energy spectrum



Meisnerron-transmon qubit

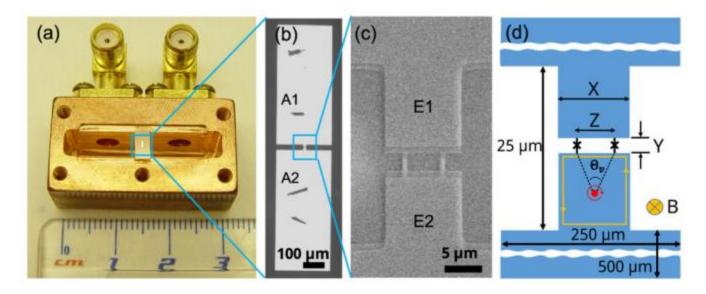
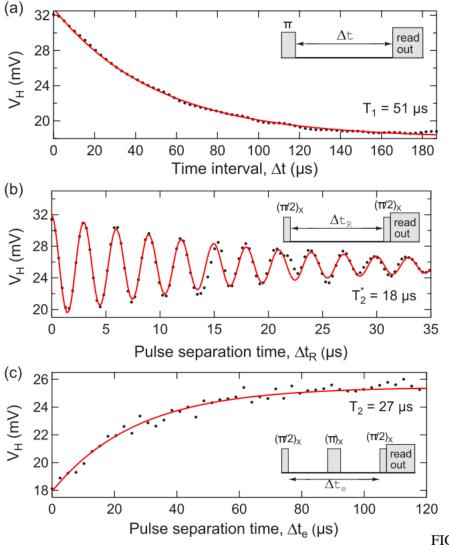


FIG. 1. (a) Optical image of the Meissner transmon qubit fabricated on a sapphire chip, which is mounted in the copper cavity. (b) A zoomed-in optical image of the qubit. Two rectangular pads marked A1 and A2 act as an RF antenna and shunt capacitor. (c) Scanning electron microscope (SEM) image of the electrodes marked E1 and E2, and a pair of JJs. (d) Schematics of the Meissner qubit. The X, Y, and Z denote the width, the distance between the electrodes, and the distance between two JJs, which are indicated by × symbols. The red dot and circular arrow around it in the bottom electrode represent a vortex and vortex current flowing clockwise, respectively. Θ_v is a polar angle defined by two dashed lines connecting the vortex and two JJs. The orange rectangular loop on the boundary of the bottom electrode indicates the Meissner current circulating counterclockwise.

Meisnerron-transmon qubit



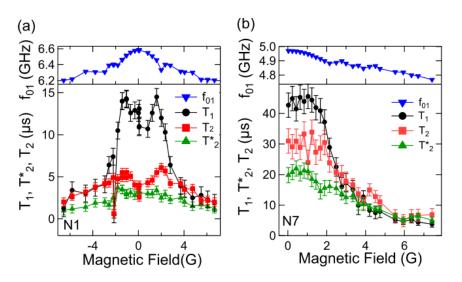


FIG. 6. The qubit transition frequencies (f_{01}) and three times scales $(T_1, T_2^*, \text{ and } T_2)$ were measured at the sweet spots over the wide range of magnetic field for the N1 (a) and N7 (b).

FIG. 4. Time domain measurements of the N7 sample at B = 7.5 mG. (a) Relaxation time measurement ($T_1 = 51 \ \mu$ s). (b) Ramsey fringe experiment ($T_2^* = 18 \ \mu$ s). (c) Hahn spin echo experiment ($T_2 = 27 \ \mu$ s). The red solid lines are the fits to the data. See the main text for the fitting functions.

J. Ku et al., PHYSICAL REVIEW B 94, 165128 (2016)

Conclusions

- Superconductivity is related to fundamental quantum phenomena. We have revied some of them. They will be discussed in more details in the future lectures.
- Superconductors have been used to create strong and stable magnetic fields, in levitating trains for example.
- Superconducting quantum interference devices enabled researches to measure very small magnetic fields, such as those produced by human brain.
- Superconductors are used to build qubits, which are the building blocks of quantum computers.